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SEAT No. :

P4872

[Total No. of Pages : 2

B.E./Insem. - 73
B.E. (Computer Engineering)
DESIGN & ANALYSIS OF ALGORITHMS
(2012 Pattern)

Time : 1 Hour]

[Max. Marks : 30

Instructions to the candidates:

- 1) *Figures to the right indicate full marks.*
- 2) *Draw neat diagram wherever necessary.*
- 3) *Make suitable assumptions wherever necessary.*

Q1) a) Solve following recurrence equation using Master Theorem. **[6]**

$$T(n) = 16 T(n/4) + n^2.$$

b) Prove the following theorem:

$$\text{If } f(n) = a_m n^m + \dots + a_1 n + a_0 \text{ and } a_m > 0,$$

$$\text{then } f(n) = O(n^m) \quad \text{[4]}$$

OR

Q2) a) Write quick sort algorithm with time complexity of this algorithm. **[6]**

b) Explain time and space complexity with suitable examples. **[4]**

Q3) a) Let No. of keys, $n = 3$ and Keys $\{k_1, k_2, k_3\} = \{\text{do, if, while}\}$

$$\text{Let Probability of successful search, } p(1:3) = \{0.5, 0.1, 0.05\}$$

$$\text{Let Probability of unsuccessful search, } q(0:3) = \{0.15, 0.1, 0.05, 0.05\}$$

Compute & construct OBST for above values. **[8]**

b) State and explain the principle of dynamic programming. Name the elements of dynamic programming. **[2]**

P.T.O.

OR

- Q4)** a) Find an optimal solution for following greedy knapsack problem:
Number of objects $n = 3$, Knapsack capacity $m = 20$, Profits $(P_1, P_2, P_3) = (25, 24, 15)$ and Weights $(W_1, W_2, W_3) = (18, 15, 10)$. [6]
- b) Write control abstraction (General Strategy Algorithm) of dynamic programming. [4]
- Q5)** a) Write an algorithm to solve 4 queen's problem using backtracking method. Use mathematical modelling to support your answer. [6]
- b) Explain how Travelling Salesperson problem is solved using branch and bound method with suitable example. [4]

OR

- Q6)** a) Write an algorithm for graph coloring problem using backtracking Method. [6]
- b) Explain in detail sum of subset problem using backtracking method with suitable example. [4]

OR

- Q7)** a) Explain all three asymptotic notations with 2 examples of each. [6]
- b) Derive worst case time complexity of following series: $n(n-1)$. [4]

